



Q5. (12 Marks) Consider a GSM system with spectrum allocation of 890-915MHz UL and 935-960MHz DL, with channel spacing of 200 kHz and a reserved guard band of 100 kHz at the beginning and the end for each of the UL and DL spectrum and 8 voice channels per digital channel.

- How many voice channels in this system?
- Calculate the cluster size  $N$  for this system if the required signal to interference ratio  $S/I$  is 14 dB and the path loss exponent  $n=4$ ? (Assume that there are 6 co-channels cells in the first tier, and all of them are at the same distance from the mobile)
- Calculate the Co-channel distance?
- What is the number of voice channels per cell in GSM under the given  $S/I$  condition?
- How many omnidirectional base stations having 2 km coverage radius are required to cover an area of 312 km<sup>2</sup>? Use the hexagonal cell shape?
- What is the maximum number of simultaneous users in the network?

Solution:

- 890-915 MHz for uplink  $\rightarrow$  25 MHz bandwidth  
935-960 MHz for downlink  $\rightarrow$  25 MHz bandwidth  
We have 25 000 KHz/200 kHz = 125 channels, one of which is reserved for guard band and 124 channels remain for users. On each channel 8 voice channels are carried by using 8 time-multiplexing.  
Total number of voice channels = 124 x 8 = 992.
- $S/I = Q_n / 6 = 1/6 (3N)^{n/2}$  ,,  
Cluster size for a given  $S/I$  is:  $N = 1/3 (6 S/I)^{2/n}$   
14 dB  $\Leftrightarrow S/I = 25.11$   
 $N = 1/3 (6 \times 25.11)^{2/4} = 4.09 \rightarrow N=7$
- Co-channel distance  $D = R \sqrt{3N} = R \sqrt{3 \times 7}$  for  $N=7$
- [124 RF channels / 7 Cells/cluster] = 18 channels per cell for 5 cells and 17 channels per cell for 2 cells.  
[124 RF channels / 7 Cells/cluster] x 8 voice channel = 136 voice channels per cell for 2 cells and 144 channels per cell for 5 cells.
- Cell area is = 2.6 R<sup>2</sup> = 2.6 x 22 = 10.4 km<sup>2</sup>  
Number of required base stations = 312/10.4 = 30 base stations
- Maximum number of simultaneous users (channels) = 136 user/cell x 30 cells = 4080 channels





Q4. (8 Marks) A cellular system with cluster size of 7, probability of blocking of 1%, average call duration of 2 minutes, each user has a call rate of 1 call per hour, and omnidirectional antenna cells with 60 traffic channels each. Assuming that blocked call cleared system is used, Find the following:

- Maximum number of users that can be supported per cell.
- Co-channel reuse ratio and frequency reuse distance, if the cell radius is 1.3 km.
- Traffic capacity loss due to trunking the traffic channels when going from omnidirectional to 60° sectored antennas.
- What is co-channel interference? And how it can be reduced?

Solution:

- $N = 7$ ,  $GOS = 1\%$ ,  $H = 2$  minutes,  $\lambda = 1$  call/hour,  $\#Ch = 60$ , Erlang B (blocked-call cleared system)  
from Erlang B table,  $A = 46.95$  erlangs  
 $A_u = H \cdot \lambda = 2 \cdot 1/60 = 1/30$  erlangs  
 $\#U_{cell} = A / A_u = 46.95 / (1/30) = 1408$  users per cell  
 $\#U_{cluster} = 1408 \cdot 7 = 9856$  users per cluster
- Co-channel reuse ratio:  $Q = D/R = \sqrt{3N} = \sqrt{3 \cdot 7} = 4.58$   
Frequency reuse distance:  $D = R \cdot Q = 1.3 \text{ km} \cdot 4.58 = 5.96 \text{ km}$
- When employing 60° sectoring, there are only 10 channels per antenna sector 60/6, So  
 $GOS = 1\%$ ,  $H = 2$  minutes,  $\lambda = 1$  call/hour,  $\#Ch = 60/6$ , from Erlang B table,  $A = 4.461$  erlangs  
 $A_u = H \cdot \lambda = 2 \cdot 1/60 = 1/30$  erlangs  
 $\#U_{sector} = A / A_u = 4.461 / (1/30) = 133$  users per sector  
 $\#U_{cell} = \#U_{sector} \cdot 6 = 133 \cdot 6 = 798$  users per cell  
 $\#U_{cluster} = 798 \cdot 7 = 5586$  users per cluster  
Traffic capacity loss when compared to the unsector case =  $1 - 798/1408 = 0.433 = 43.3\%$   
Thus, sectoring decreases the trunking efficiency while improving the S/I for each user in the system.
- The interference between signals from co-channel cells (cells that use the same set of frequencies) is called co-channel interference.  
Co-channel interference can be reduced by using:
  - directional antennas (Cell sectoring)
  - Adaptive Power Control



(يسمح للطلاب بإدخال ورقة قوانين جهة واحدة A4 وجداول Erlang مع ضرورة كتابة الاسم عليها وتسليمها مع كراسة الاجابة)

**Q1. (6 Marks)** A satellite at a distance of 40000 km from an earth station radiates a power of 3 W from an antenna with a gain of 15 dB in the direction of the earth station. If the receiving antenna has an effective area of 10 m<sup>2</sup> and the receiver has a noise temperature of 500 K. Calculate the C/No ratio in dB at the receiver?

**Solution:**

$$\text{Flux density: } F = \text{EIRP} - 10\log(4\pi d^2) = 10\log(3) + 15 - 10\log(4\pi(40000e3)^2) = -143.2621 \text{ dBW/m}^2$$

$$\text{Power received: } Pr = \text{EIRP} / (4\pi d^2) * A_{\text{eff}} = F + 10\log(A_{\text{eff}}) = -143.26 + 10\log(10) = -133.2621 \text{ dBW}$$

$$\text{Noise power density: } No = kT = 10\log(1.38 \times 10^{-23} \times 500) = -201.6115 \text{ dBW}$$

$$C/No = Pr - No = -133.2621 + 201.6115 = 68.3494 \text{ dB.}$$

**Q2. (6 Marks)** An earth station antenna is located at 89°W longitude and 35°N latitude. It is intended to transmit and receive signals to a satellite in geostationary orbit at 82°W longitude and height of 38000 km. Calculate the intermediate angle from earth station?

**Solution:**

$$\text{Intermediate angle } (\alpha) = \tan^{-1}[\tan(|l_s - l_e|) / \sin(L_e)] = \tan^{-1}[\tan(|82 - 89|) / \sin(35)] = 12.0828^\circ.$$

**Q3. (6 Marks)** Derive the co-channel reuse ratio for a hexagonal geometry, where  $N = i^2 + ij + j^2$  is used to find the nearest co-channel neighbors for a particular cell?

**Solution:**

have

$$D = [i(2R')]^2 + [j(2R')]^2 - 2i(2R') \cdot j(2R') \cdot \cos(120^\circ)$$

$$\text{where } R' = \frac{\sqrt{3}}{2} R, \text{ therefore}$$

$$D = \sqrt{3i^2 R^2 + 3j^2 R^2 + ij \cdot 3R^2}$$

$$= \sqrt{3(i^2 + ij + j^2)} \cdot R$$

$$= \sqrt{3N} \cdot R$$

$$\text{Hence, } G = \frac{D}{R} = \sqrt{3N}$$

